

Time: (03) hours

Total Marks: 100

N.B. (i) Question no. ONE is compulsory.

(ii) Attempt any FOUR questions from remaining six questions.

(iii) Figures to right indicate full marks.

- Q.1 (a) Evaluate 3  

$$\int_0^{\pi/6} \cos^3 3\theta \sin^2 6\theta d\theta$$
- (b) Solve 3  

$$\frac{d^3 y}{dx^3} + 2\frac{d^2 y}{dx^2} - 5\frac{dy}{dx} - 6y = 0$$
- (c) Evaluate 3  

$$\int_{-1}^1 \int_0^{x+z} \int_0^{x-z} (x+y+z) dy dx dz$$
- (d) Evaluate 3  

$$\int_1^2 \int_0^x \frac{1}{x^2 + y^2} dy dx$$
- (e) Solve  $(2x^2 + 3y^2 - 7)xdx + (3x^2 + 2y^2 - 8)ydy = 0$  4
- (f) Using Euler's method find the approximate value of  $y$  where 4  
 $\frac{dy}{dx} = x + 2y$ ,  $y(1) = 1$  taking  $h = 0.2$  at  $x = 2$
- Q.2 (a) Evaluate 6  

$$\int_0^{\pi/2} \int_0^{1-\sin\theta} r^2 \cos\theta dr d\theta$$
- (b) Evaluate  $\iiint (x + y + z) dx dy dz$  over the tetrahedron bounded by the 6  
 planes  $x = 0, y = 0, z = 0$  and  $x + y + z = 1$
- (c) Show that 8  

$$\int_0^{\infty} \frac{\tan^{-1}(x/a) - \tan^{-1}(x/b)}{x} dx = \frac{\pi}{2} \log\left(\frac{b}{a}\right) \text{ where } a > 0, b > a$$
- Q.3 (a) Solve 6  

$$\tan y \frac{dy}{dx} + \tan x = \cos y \cos^3 x$$

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(2)

- (b) Find by double integration the area between the curves 6

$$y^2 = 4x \text{ and } 2x - 3y + 4 = 0$$

- © Solve 8

$$\frac{d^2y}{dx^2} + 9y = e^x - \cos 2x$$

- Q.4 (a) Solve 6

$$(4xy + 3y^2 - x)dx + x(x + 2y)dy = 0$$

- (b) Change the order of integration and evaluate 6

$$\int_0^1 \int_0^{\sqrt{1-x^2}} \frac{e^{-y}}{(e^y + 1)\sqrt{1-x^2-y^2}} dy dx$$

- © Using Taylor's series method solve the differential equation 8

$$\frac{dy}{dx} = x + y, \text{ start from } x = 1, y = 0 \text{ and carry to } x = 1.2 \text{ with } h = 0.1$$

- Q.5 (a) Find the length of one arc of the cycloid  $x = a(\theta - \sin \theta), y = a(1 + \cos \theta)$  6

- (b) Find the volume bounded by the cylinder  $x^2 + y^2 = a^2$  and the planes  $z = 0$  and  $y + z = b$  6

- © Solve numerically using Runge - Kutta Method of Fourth order the differential equation  $\frac{dy}{dx} = xy$  with initial conditions  $y(1) = 1$  at  $x = 1.2$  8

taking  $h = 0.1$

- Q.6 (a) Evaluate 6

$$\int_0^1 x^{q-1} \left( \log \frac{1}{x} \right)^{p-1} dx$$

- (b) Evaluate 6

$$\iint (x^2 - y^2) x dx dy \text{ over the positive quadrant of the circle } x^2 + y^2 = a^2$$

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(3)

(c) Solve by method of variation of parameters  $(D^2 + a^2)y = \sec ax$  8

Q.7 (a) Evaluate 6

$$\int_0^1 x^6 (1-x^2)^{1/2} dx$$

(b) Change to polar coordinates and evaluate  $\int_0^a \int_0^a x dx dy$  6

(c) The charge  $q$  on the plate of a condenser of capacity  $C$  charged through a resistance  $R$  by a steady voltage  $V$  satisfies the differential equation  $R \frac{dq}{dt} + \frac{q}{C} = V$ . If  $q = 0$  at  $t = 0$ , show that  $q = CV(1 - e^{-t/RC})$ . Find also the current flowing into the plate. 8

(3 Hours)

Total Marks: 100

**N.B.:** (1) Question No. 1 is compulsory.

(2) Attempt any four questions out of remaining six questions.

Q1. a) What are constructors? Explain different types of constructors with example. [10]  
 b) Write a program in java to check whether the given string is palindrome or not. [10]

Q2. a) Explain life cycle of a thread. [10]  
 b) Write short note on thread synchronization. [10]

Q3. a) What is vector? How it is different from an array? [10]  
 b) Explain exception handling in java with example. [10]

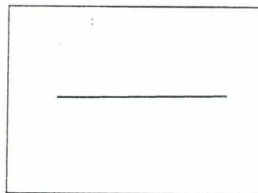
Q4. a) Write a program in java to display the following pattern: [10]

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A
A   B
A   B   C
A   B   C   D
  
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b) Write a program in java to find factorial of a given number. [10]

Q5. a) Write an applet to display the following: [10]



b) What is command line argument? Write a program in java to find largest of two numbers accepted from command line. [10]

Q6. a) Explain how java supports multiple inheritance with example. [10]

b) Write a program in java to find largest of three numbers accepted from command line. [10]

Q7. Write short note on (any two) [20]

- Life cycle of a thread
- Call by value and Call by reference
- Wrapper class
- Access protection in java

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