



3501 (MAN)-1/2018

**AKTC KALSEKAR TECHNICAL CAMPUS**

INNOVATIVE TEACHING FREQUENT LEARNING

School of Architecture

School of Engineering & Technology

School of Pharmacy

*Knowledge Resource & Relay Centre (KRRC)*

AIKTC/KRRC/SoET/ACKN/QUES/2018-19/

Date: \_\_\_\_\_

School: SoET-CBSGS

Branch: EXTC ENGG.

SEM: III

To,  
Exam Controller,  
AIKTC, New Panvel.

Dear Sir/Madam,

Received with thanks the following <sup>✓</sup>Semester/Unit Test-I/Unit Test-II (Reg./ATKT) question papers from your exam cell:

Sr. No.	Subject Name	Subject Code	Format		No. of Copies
			SC	HC	
1	Applied Mathematics- III	ETS301		✓	02
2	Analog Electronics – I	ETC302			
3	Digital Electronics	ETC303			
4	Circuits & Transmission Lines	ETC304		✓	02
5	Electronics Instruments & Measurement	ETC305			

Note: SC – Softcopy, HC - Hardcopy

(Shaheen Ansari)  
Librarian, AIKTC

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22-11-17-11 - 13343 - EXTC - ERMCAJ

14/5/19

( 3 Hours)

[ Total marks : 80

- Note :-
- 1) Question number 1 is compulsory.
  - 2) Attempt any three questions from the remaining five questions.
  - 3) Figures to the right indicate full marks.

- Q.1
- a) Find the Laplace transform of  $\sinh^5 t$ , 05
  - b) Find an analytic function whose imaginary part is  $e^{-x}(y \cos y - x \sin y)$ , 05
  - c) Find the Fourier series for  $f(x) = 1 - x^2$  in  $(-1, 1)$ . 05
  - d) Evaluate  $\int_C \vec{F} \cdot d\vec{r}$  where  $\vec{F} = 2x i + (xz - y) j + 2z k$  from  $O(0, 0, 0)$  to  $P(3, 1, 2)$  along the line  $OP$ . 05
- Q.2
- a) Find a cosine series of period  $2\pi$  to represent  $\sin x$  in  $0 \leq x \leq \pi$ . 06
  - b) Find  $a, b, c$  if  $\vec{F} = (axy + bz^3) i + (3x^2 - cz) j + (3xz^2 - y) k$  is irrotational. 06
  - c) Find the image of the circle  $|z| = k$  where  $k$  is real under the bilinear transformation  $w = \frac{5-4z}{4z-3}$ . 08
- Q.3
- a) Prove that  $J_{\frac{1}{2}}(x) = \tan x \cdot J_{-\frac{1}{2}}(x)$ . 06
  - b) Find the inverse Laplace transform of the following function by convolution theorem 06  

$$\frac{(s+2)^2}{(x^2+4s+8)^2}$$
  - c) Obtain the complex form of Fourier series for  $f(x) = e^{ax}$  in  $(-l, l)$  where  $a$  is not an integer. 08
- Q.4
- a) Find the angle between the normals to the surface  $xy = z^2$  at the points  $(1, 4, 2)$  and  $(-3, -3, 3)$ . 06
  - b) Prove that 06  

$$x^2 J_n''(x) = (n^2 - n - x^2) J_n(x) + x J_{n+1}(x);$$

$$n = 0, 1, 2, \dots$$

- e)
- (i) Find the Laplace transform of  $\sinh at \sin at$ . 04
- (ii) Find the Laplace transform of  $te^{-4t} \sin 3t$ . 04
- Q.5 a) Prove that  $J_2(x) = J_0''(x) - \frac{J_0'(x)}{x}$ . 06
- b) If  $v = e^x \sin y$ , show that  $v$  is harmonic and find the corresponding analytic function. 06
- c) Find the Fourier series for  $f(x)$  in  $(0, 2\pi)$ , 08
- $$f(x) = \begin{cases} x, & 0 < x \leq \pi \\ 2\pi - x, & \pi \leq x < 2\pi \end{cases}$$
- Hence, deduce that
- $$\frac{\pi^4}{96} = \frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots$$
- Q.6 a) Show that the set of functions  $\cos nx$ ,  $n = 1, 2, 3, \dots$  is orthogonal on  $(0, 2\pi)$ . 06
- b) Using Green's theorem evaluate  $\int_C \vec{F} \cdot d\vec{r}$  where  $C$  is the curve enclosing the region bounded by  $y^2 = 4ax$ ,  $x = a$  in the plane  $z = 0$  and
- $$\vec{F} = (2x^2y + 3z^2) i + (x^2 + 4yz) j + (2y^2 + 6xz) k.$$
- c) Use Laplace transform to solve 08
- $$\frac{d^2y}{dt^2} + 4 \frac{dy}{dt} + 8y = 1 \text{ with } y(0) = 0, y'(0) = 1.$$

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Time: 3 Hours

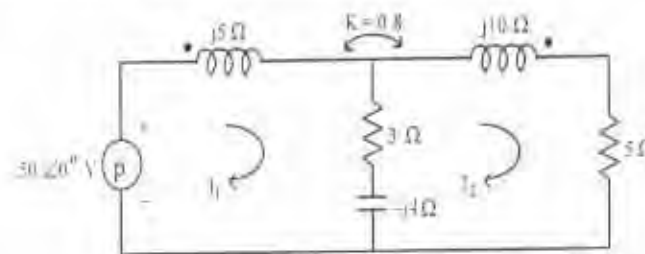
Total Marks: 80

N.B.

- 1) Question No. 1 is Compulsory
- 2) Out of remaining questions, attempt any three
- 3) Assume suitable data if required
- 4) Figures to the right indicate full marks

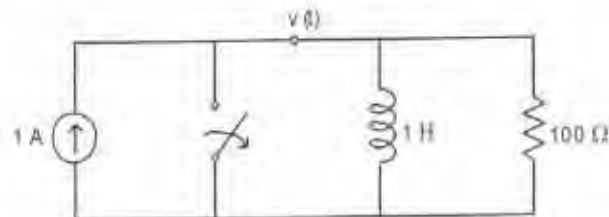
1 (A) Draw equivalent circuit for given magnetically coupled circuit.

05

(B) In the network shown in Fig., at  $t = 0$ , switch is opened. Calculate  $v$ ,  $\frac{dv}{dt}$  at  $t =$ 

05

00.

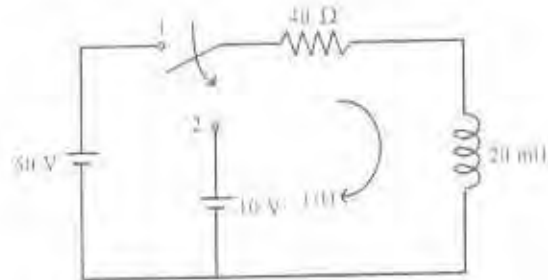
(C) The Z parameters of a 2 port network are,  $Z_{11} = 20 \Omega$ ,  $Z_{22} = 30 \Omega$ ,  $Z_{12} = Z_{21} = 10 \Omega$ . Find Y parameters.

05

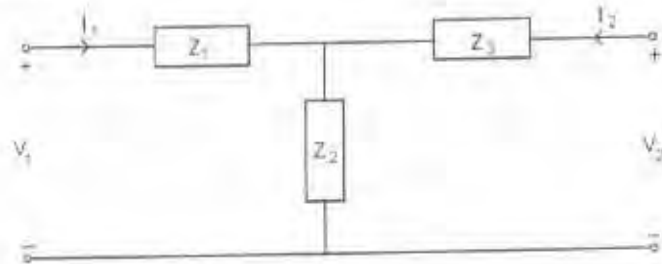
(D) Two two port networks are connected in parallel. Prove that the sum of the corresponding individual parameters is equal to the overall y parameters.

05

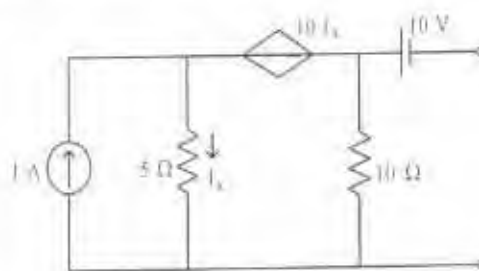
- 2 (A) The network of Fig. is under steady state with switch at position 1. At  $t = 0$ , switch is moved to position 2. Find  $i(t)$ . 10



- (B) The Z-parameters of a two port are :  $Z_{11} = 20 \Omega$ ,  $Z_{12} = Z_{21} = 10 \Omega$ ,  $Z_{22} = 30 \Omega$ . Find equivalent T-network. 10



- 3 (A) Determine Thevenin's equivalent network for the Fig. shown. 10



- (B) The parameters of a transmission lines are  $R = 65 \Omega/\text{km}$ ,  $L = 1.6 \text{ mH}/\text{km}$ ,  $G = 2.25 \times 10^{-4} \text{ S}/\text{km}$ ,  $C = 0.1 \mu\text{F}/\text{km}$ . Find  
 i) Characteristic Impedance

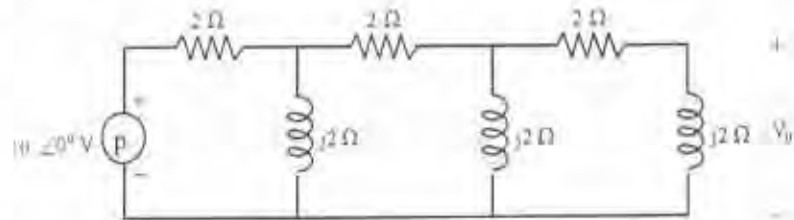
- ii) Propagation Constant
- iii) Attenuation Constant
- iv) Phase Constant at 1 kHz

4 (A) Determine whether following functions are positive real 10

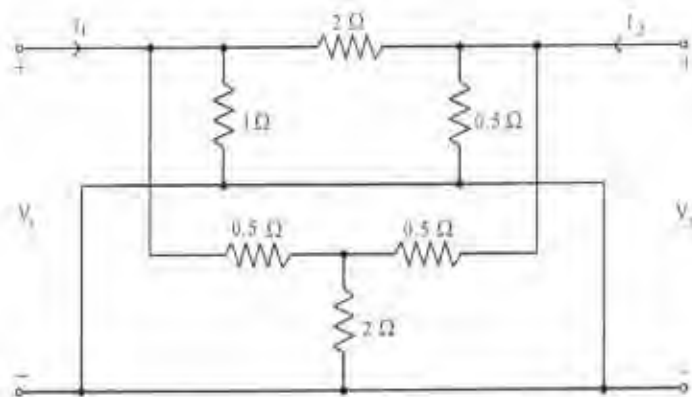
i)  $\frac{s^4 + 2s^3 + 3s^2 + 1}{s^4 + s^3 + 3s^2 + 2s + 1}$

ii)  $\frac{s^2 + 2s}{s^2 + 1}$

(B) In the network of Fig, find  $V_o$ . 10



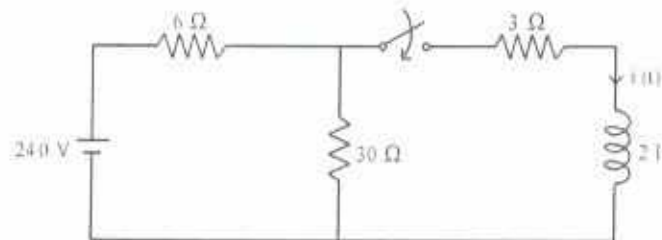
5 (A) Find Y-parameters for the network shown in Fig 10



(B) Realize the following functions in Foster I and Foster II form 10

$$F(s) = \frac{4(s+1)(s+3)}{(s+2)(s+6)}$$

6. (A) A transmission line has a characteristics impedance of 50 ohm and terminate in a load  $Z_L = 25 + j50$  ohm. Use smith chart and Find VSWR and Reflection coefficient at the load. 10
- (B) The switch in Fig. is open for a long time and closes at  $t = 0$ . Determine  $i(t)$  for  $t > 0$ . 10



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