SE- SEM-III - REV- CE/MECH

14/05/15

Q.P. Code: 4755

Total Marks: 80 (3 Hours)

Question No. 1 is compulsory. N.B.: (1)

- Attempt any three questions out of remaining five questions.
- (a) Find the Laplace transform of te-t cosh2t

5

Find the fixed points of $w = \frac{3z-4}{z-1}$. Also express it in the normal form

 $\frac{1}{w-\alpha} = \frac{1}{z-\alpha} + \lambda$ where λ is a constant and α is the fixed point. Is this

transformation parabolic?

- Evaluate $\int_{0}^{1+1} (x^2-iy)dz$ along the path i) y=x, ii) y=x² (c) 5
- Prove that $f_1(x)=1$, $f_2(x)=x$, $f_3(x)=\frac{3x^2-1}{2}$ are orthogonal over (-1,1) 5 (d)
- Find inverse Laplace transform of $\frac{2s}{s^4 + 4}$ (a) 6
 - Find the image of the triangular region whose vertices are i, 1+i, 1-i under (b) 6 the transformation w = z + 4-2i. Draw the sketch.
 - 8 Obtain fourier expansion of $f(x) = |\cos x|$ in $(-\pi, \pi)$. (c)
- Obtain complex form of fourier series for $f(x) = \cosh 2x + \sinh 2x$ in (-2,2). (a)
 - Using Carnk-Nicholson simplified formula solve $\frac{\partial^2 u}{\partial x^2} \frac{\partial u}{\partial t} = 0$ given (b)

u(0,t) = 0, u(4, t) = 0, $u(x, 0) = \frac{x}{3}$ (16-x²) find uij for i=0,1,2,3,4 and j=0, 1,2

(c) Solve the equation $y + \int_{0}^{\infty} y dt = 1 - e^{-t}$ 8 2

4. (a) Evaluate $\int_{0}^{2\pi} \frac{d\theta}{5 + 3\sin\theta}$

- (b) Find half range cosine series for $f(x)=e^x$, 0 < x < 1
- (c) Obtain two distinct Laurent's series for $f(z) = \frac{2z-3}{z^2-4z-3}$ in powers of 8 (z-4) indicating the regions of convergence.
- 5. (a) Solve $\frac{\partial^2 u}{\partial x^2} 2\frac{\partial u}{\partial t} = 0$ by Bender Schmidt method, given u(0, t) = 0, u(4, t) = 0, u(x,0) = x(4-x). Assume h=1 and find the values of u upto t = 5
 - (b) Find the Laplace transform of e^{-4t} ∫ usin3udu 6
 - (c) Evaluate $\int_{C} \frac{z+3}{z^2+2z+5}$ dz where C is the circle i) |z|=1, ii) |z+1-i|=2
- 6. (a) Find inverse Laplace transform of $\frac{s}{(s^2-a^2)^2}$ by using convolution theorem. 6
 - (b) Find an analytic function f(z) = u+iv where $u+v=e^x (cosy + siny)$
 - (c) Solve the equation $\frac{\partial u}{\partial t} = k \frac{\partial^2 u}{\partial^2 x^2}$ for the conduction of heat along a rod of 8

(i) u is not infinity for $t \rightarrow \infty$

(ii) $\frac{\partial \mathbf{u}}{\partial \mathbf{x}} = 0$ for $\mathbf{x} = 0$ and $\mathbf{x} = l$ for any time t

length l subject to following conditions

(iii) $u=lx-x^2$ for t=0 between x=0 and x=l
