

Time 03 hours.

Max Marks: 80

Instructions to candidate

1. Q 1 is compulsory
2. Attempt any THREE from remaining
3. Figures to the right indicate full marks
4. Assume suitable data if necessary

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|---|---|----|
| 1 | a] Explain concept of power spectral density | 5 |
| | b] state and prove Central Limit Theorem | 5 |
| | c] Explain properties of cross correlation function | 5 |
| | d]state and prove Bayes' theorem | 5 |
| 2 | a] Box 1 contains 5 white balls and 6 black balls. Box 2 contains 6 white & 4 black balls | 10 |
| | A box is selected at random and then a ball is chosen at random from the selected | |
| | Box (i)What is the probability that the ball chosen will be a white ball | |
| | (ii)Given that the ball chosen is white what is the probability that came from box1 | |
| | b] Give the properties of CDF, pdf, and PMF. | 10 |
| 3 | a] Explain concept of conditional probability and properties of conditional probability | 10 |
| | b] Explain what do you mean by? | 03 |
| | (i)Deterministic system | |
| | (ii) stochastic system | |
| | (iii) Memoryless system | |
| | c] Prove that if input to memoryless system is strict sense stationary(SSS) process then | 07 |
| | output is also strict sense stationary | |
| 4 | a] Explain Random process, define ensemble mean, Auto correlation, and Auto covariance of | |
| | the process in terms of indexed random variables in usual mathematical forms | 10 |
| | b] Let $Z=X+Y$ Determine pdf of Z $f_z(Z)$ | 10 |
| 5 | a] state and prove Chapman Kolmogorov equation | 10 |
| | b] Explain Chebyshev's Inequality with suitable example. | 10 |

TURN OVER

6] a) The joint probability density function of two random variables is given by

$$F_{xy}(x, Y) = 15 e^{-3x-3y} ; x \geq 0, y \geq 0$$

- i) Find the probability that $x < 2$ and $Y > 0.2$
- ii) Find the marginal densities of X and Y
- iii) Are X and Y Independent?
- iv) Find $E(x/y)$ and $E(y/x)$

10

b) Write short Notes on following special distributions

- i) Poisson distributions ii) Rayleigh distributions iii) Gaussian distributions

10

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