



ANJAYAMMILALAYAR

AIKTC KALSEKAR TECHNICAL CAMPUS

INNOVATIVE TEACHING | SUBSTANTIVE LEARNING

School of Architecture

School of Engineering & Technology

School of Pharmacy

Knowledge Resource & Relay Centre (KRRC)

AIKTC/KRRC/SoET/ACKN/QUES/2018-19/

Date: _____

School: SoET-CBSGS

Branch: ELECT. ENGG.

SEM: IV

To,
Exam Controller,
AIKTC, New Panvel.

Dear Sir/Madam,

Received with thanks the following [✓]Semester/[✓]Unit Test-I/Unit Test-II (Reg./ATKT) question papers from your exam cell:

Sr. No.	Subject Name	Subject Code	Format		No. of Copies
			SC	HC	
1	Applied Mathematics- IV	EEC401		✓	02
2	Elements Of Power System	EEC402			
3	Electrical Machines – I	EEC403			
4	Signal Processing	EEC404			
5	Analog And Digital Integrated Circuits	EEC405			
6	Numerical Methods & Optimization Techniques	EEC406			

Note: SC – Softcopy, HC - Hardcopy

(Shaheen Ansari)
Librarian, AIKTC

10-15

Paper / Subject Code: 39002 / APPLIED MATHEMATICS - IV

Duration: 3 Hours

Marks: 80

N.B: a) Question number 1 is compulsory

b) Solve any three from the remaining.

c) All the question carry equal marks

1. a) Find the extremal of $\int_0^\pi \frac{1+y^2}{y'^2} dx$ subject to $y(0) = 0, y(\pi) = 0$. [5]

b) Using Cauchy's Schwartz Inequality, show that $(a \cos \theta + b \sin \theta)^2 \leq a^2 + b^2$,
Where 'a' and 'b' are real. [5]

c) Show that Eigen values of Hermitian matrix are real. [5]

d) Evaluate $\int (z^2 - 2\bar{z} + 1) dz$ over a closed circle $x^2 + y^2 = 2$. [5]

2. a) Find the extremal $\int_{x_1}^{x_2} (y'^2 - y'^2 - 2y \cosh x) dx$ [6]

b) Find the Eigen values and Eigen Vectors of the matrix $A^2 + 3I$, where [6]

$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$

c) Obtain all possible expansion of $f(z) = \frac{1}{z^2(z-1)(z+2)}$ about $z = 0$ indicating region of convergence. [8]

3. a) Verify Cayley - Hamilton Theorem for $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & -2 \\ -2 & 0 & 1 \end{bmatrix}$ and find A^{-1} . [6]

b) Using Residue theorem evaluate $\int \frac{e^z}{z^2 + \pi^2} dz$ where C is $|z| = 4$. [6]

c) Show that a closed curve 'C' of a given fixed length (perimeter) which encloses maximum area is a circle. [8]

4. a) Find an orthonormal basis for the subspace of R^3 by applying Gram-Schmidt process, where $u_1 = (1,0,0), u_2 = (3,7,-2), u_3 = (0,4,1)$. [6]

b) Find A^{50} for the matrix $A = \begin{bmatrix} 4 & 3 \\ 7 & 8 \end{bmatrix}$ [6]

- c) Reduce the Quadratic Form $xy + yz + zx$ to normal form by congruent transformation. [8]
5. a) Using Rayleigh-Ritz Method, find an approximate solution to the extremal problem $\int_0^1 (y'^2 + 2yx - y'^2) dx$, $y(0) = 0$, $y(1) = 0$. [6]
- b) Determine whether the set $V = \{(x, y, z); x = 1, y = 0 \text{ or } z = 0\}$ is a subspace of R^3 . [6]
- c) Show that the matrix $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ is diagonalizable. Also find the transforming matrix and diagonal matrix. [8]
6. a) Using Cauchy's Residue Theorem, evaluate $\int_0^{2\pi} \frac{d\theta}{2 + \cos\theta}$. [6]
- b) Evaluate $\int_{1-i}^{2+i} (2x + 1 + iy) dx$ along the straight line joining $A(1, -1)$ and $B(2, 1)$. [6]
- c) Find the singular value decomposition of the matrix $A = \begin{bmatrix} 2 & 3 \\ 0 & 2 \end{bmatrix}$. [8]
